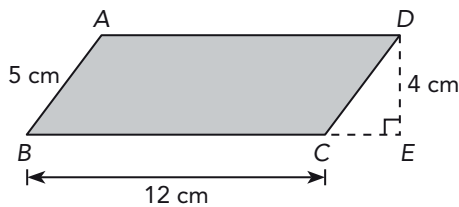


Lesson 10.2 Area of Parallelograms and Trapezoids

Find the area of each parallelogram.

Example

In the figure, $ABCD$ is a parallelogram. Find the area of parallelogram $ABCD$.



Base = BC = 12 cm

Height = DE = 4 cm

Area of parallelogram $ABCD = bh$

$$= 12 \cdot 4$$

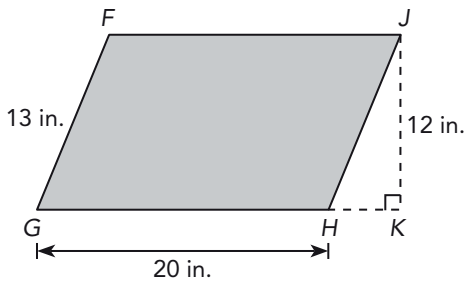
$$= 48 \text{ cm}^2$$

The area of parallelogram $ABCD$ is 48 square centimeters.

In parallelogram $ABCD$, DE is the height, because it is perpendicular to base BC .



1. In the figure, $FGHJ$ is a parallelogram. Find the area of parallelogram $FGHJ$.



Base = _____ = _____ in.

Height = _____ = _____ in.

Area of parallelogram $FGHJ = bh$

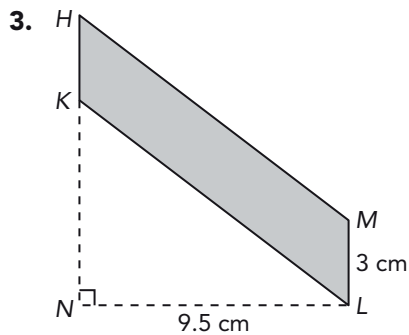
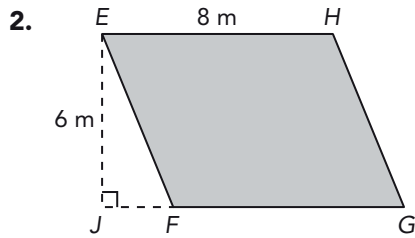
$$= \underline{\hspace{2cm}} \cdot \underline{\hspace{2cm}}$$

$$= \underline{\hspace{2cm}} \text{ in.}^2$$

The area of parallelogram $FGHJ$ is _____ square inches.

Name: _____

Date: _____



Find the area of each trapezoid.

Example

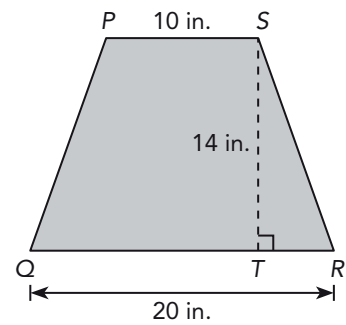
In the figure, $PQRS$ is a trapezoid. \overline{PS} is parallel to \overline{QR} . ST is the height of the trapezoid. Find the area of $PQRS$.

Height = \underline{ST} = $\underline{14}$ in.

Sum of bases = $\frac{PS}{\quad} + \frac{QR}{\quad}$
 = $\frac{10}{\quad} + \frac{20}{\quad}$
 = $\underline{30}$ in.

Area of trapezoid $PQRS$ = $\frac{1}{2}h(b_1 + b_2)$
 = $\frac{1}{2} \cdot \underline{14} \cdot \underline{30}$
 = $\underline{210}$ in.²

The area of trapezoid $PQRS$ is $\underline{210}$ square inches.



The bases of a trapezoid are parallel.

Name: _____

Date: _____

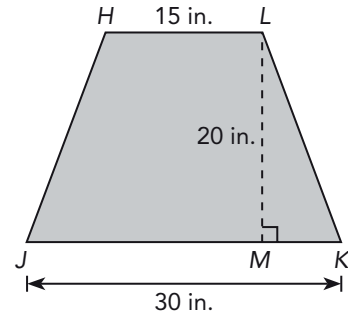
4. In the figure, $HJKL$ is a trapezoid. \overline{HL} is parallel to \overline{JK} . LM is the height of the trapezoid. Find the area of $HJKL$.

Height = _____ = _____ in.

Sum of bases = _____ + _____

= _____ + _____

= _____ in.

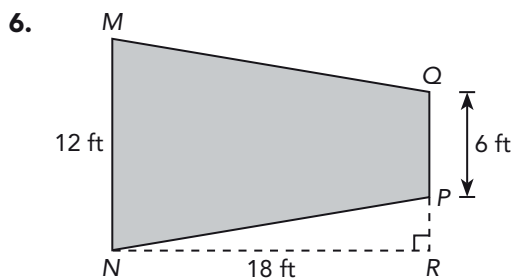
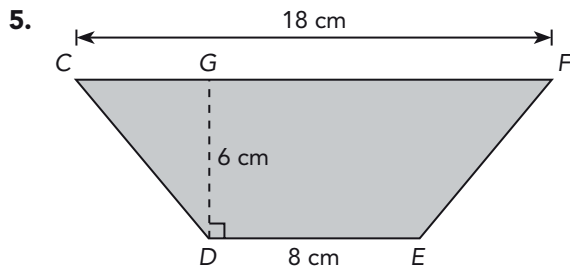


Area of trapezoid $HJKL = \frac{1}{2}h(b_1 + b_2)$

= $\frac{1}{2} \cdot$ _____ \cdot _____

= _____ in.²

The area of trapezoid $HJKL$ is _____ square inches.



Find the area of each trapezoid.

Example

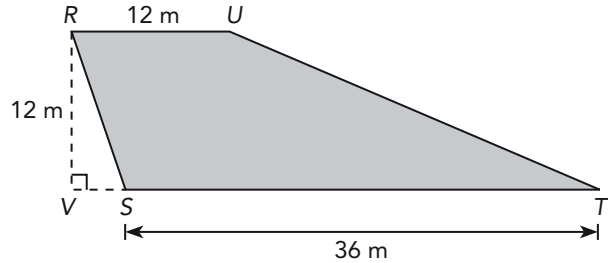
In the figure, $RSTU$ is a trapezoid. \overline{RU} is parallel to \overline{ST} . RV is the height of the trapezoid. Find the area of $RSTU$.

Height = \underline{RV} = $\underline{12}$ m

Sum of bases = \underline{RU} + \underline{ST}
 = $\underline{12}$ + $\underline{36}$
 = $\underline{48}$ m

Area of trapezoid $RSTU$ = $\frac{1}{2}h(b_1 + b_2)$
 = $\frac{1}{2} \cdot \underline{12} \cdot \underline{48}$
 = $\underline{288}$ m²

The area of trapezoid $RSTU$ is $\underline{288}$ square meters.



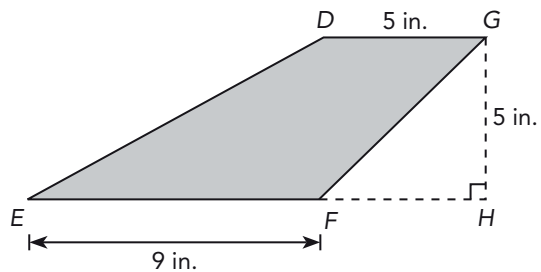
7. In the figure, $DEFG$ is a trapezoid. \overline{DG} is parallel to \overline{EF} . GH is the height of the trapezoid. Find the area of $DEFG$.

Height = _____ = _____ in.

Sum of bases = _____ + _____
 = _____ + _____
 = _____ in.

Area of trapezoid $DEFG$ = $\frac{1}{2}h(b_1 + b_2)$
 = $\frac{1}{2} \cdot$ _____ \cdot _____
 = _____ in.²

The area of trapezoid $DEFG$ is _____ square inches.



Find the height of each trapezoid.

Example

The area of trapezoid $QRST$ is 810 square feet. \overline{QT} is parallel to \overline{RS} . Find the height of the trapezoid.

Area of trapezoid $QRST = \frac{1}{2}h(b_1 + b_2)$

$$\frac{810}{2} = \frac{1}{2} \cdot h \cdot (\underline{26} + \underline{34})$$

$$\frac{810}{2} = \frac{1}{2} \cdot h \cdot \underline{60}$$

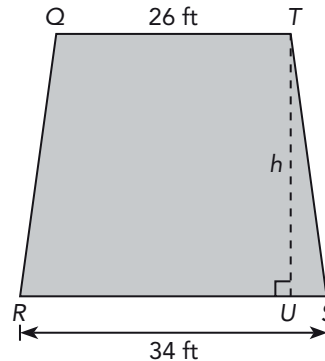
$$\frac{810}{2} = \frac{1}{2} \cdot \underline{60} \cdot h$$

$$\frac{810}{2} = \underline{30} \cdot h$$

$$\frac{810}{30} \div \frac{30}{30} = \frac{30}{30} \cdot h \div \frac{30}{30}$$

$$\underline{27} = h$$

The height of trapezoid $QRST$ is 27 feet.



8. The area of trapezoid $WXYZ$ is 540 square inches. \overline{WZ} is parallel to \overline{XY} . Find the height of the trapezoid.

Area of trapezoid $WXYZ = \frac{1}{2}h(b_1 + b_2)$

$$\underline{\hspace{2cm}} = \frac{1}{2} \cdot h \cdot (\underline{\hspace{2cm}} + \underline{\hspace{2cm}})$$

$$\underline{\hspace{2cm}} = \frac{1}{2} \cdot h \cdot \underline{\hspace{2cm}}$$

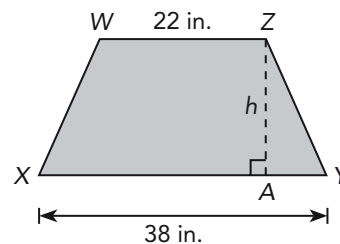
$$\underline{\hspace{2cm}} = \frac{1}{2} \cdot \underline{\hspace{2cm}} \cdot h$$

$$\underline{\hspace{2cm}} = \underline{\hspace{2cm}} \cdot h$$

$$\underline{\hspace{2cm}} \div \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \cdot h \div \underline{\hspace{2cm}}$$

$$\underline{\hspace{2cm}} = h$$

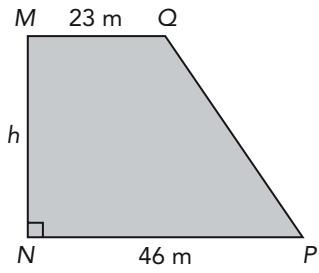
The height of trapezoid $WXYZ$ is _____ inches.



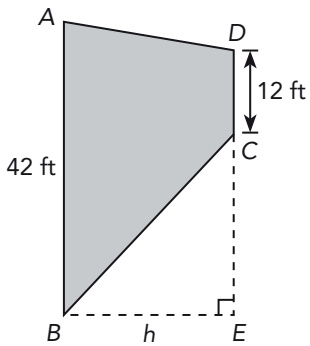
Name: _____

Date: _____

9. The area of trapezoid $MNPQ$ is 1,173 square meters.

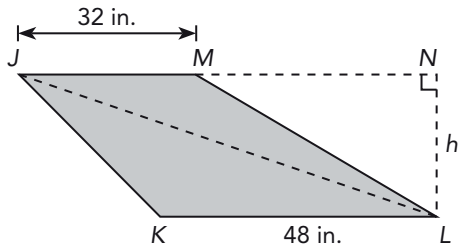


10. The area of trapezoid $ABCD$ is 621 square feet.



Solve. Show your work.*Example*

The area of trapezoid $JKLM$ is 1,000 square inches. \overline{JM} is parallel to \overline{KL} .



- a) Find the height of trapezoid $JKLM$.

$$\text{Area of trapezoid } JKLM = \frac{1}{2}h(b_1 + b_2)$$

$$\frac{1,000}{1} = \frac{1}{2} \cdot h \cdot \left(\frac{32}{1} + \frac{48}{1} \right)$$

$$\frac{1,000}{1} = \frac{1}{2} \cdot h \cdot \frac{80}{1}$$

$$\frac{1,000}{1} = \frac{1}{2} \cdot \frac{80}{1} \cdot h$$

$$\frac{1,000}{1} = \frac{40}{1} \cdot h$$

$$\frac{1,000}{1} \div \frac{40}{1} = \frac{40}{1} \cdot h \div \frac{40}{1}$$

$$\frac{25}{1} = h$$

The height of trapezoid $JKLM$ is 25 inches.

- b) Find the area of triangle JLM .

$$\text{Height of triangle } JLM = \underline{NL} = \underline{25} \text{ in.}$$

$$\text{Area of triangle } JLM = \frac{1}{2}bh$$

$$= \frac{1}{2} \cdot \frac{32}{1} \cdot \frac{25}{1}$$

$$= \frac{400}{1} \text{ in.}^2$$

The area of triangle JLM is 400 square inches.

Trapezoid $JKLM$ has the same height, NL , as triangle JLM .

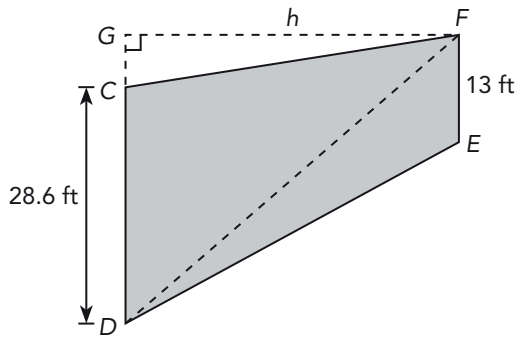


Name: _____

Date: _____



11. The area of trapezoid $CDEF$ is 832 square feet. \overline{CD} is parallel to \overline{FE} .



a) Find the height of trapezoid $CDEF$.

$$\text{Area of trapezoid } CDEF = \frac{1}{2}h(b_1 + b_2)$$

$$\underline{\hspace{2cm}} = \frac{1}{2} \cdot h \cdot (\underline{\hspace{2cm}} + \underline{\hspace{2cm}})$$

$$\underline{\hspace{2cm}} = \frac{1}{2} \cdot h \cdot \underline{\hspace{2cm}}$$

$$\underline{\hspace{2cm}} = \frac{1}{2} \cdot \underline{\hspace{2cm}} \cdot h$$

$$\underline{\hspace{2cm}} = \underline{\hspace{2cm}} \cdot h$$

$$\underline{\hspace{2cm}} \div \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \cdot h \div \underline{\hspace{2cm}}$$

$$\underline{\hspace{2cm}} = h$$

The height of trapezoid $CDEF$ is _____ feet.

b) Find the area of triangle FDE .

$$\text{Area of triangle } FDE = \frac{1}{2}bh$$

$$= \frac{1}{2} \cdot \underline{\hspace{2cm}} \cdot \underline{\hspace{2cm}}$$

$$= \underline{\hspace{2cm}} \text{ ft}^2$$

The area of triangle FDE is _____ square feet.

3. trapezoid
 \overline{PS} is parallel to \overline{QR} .
4. parallelogram
 \overline{AD} is parallel to \overline{BC} .
 \overline{AB} is parallel to \overline{DC} .
5. trapezoid
 \overline{DG} is parallel to \overline{EF} .
6. rhombus
 \overline{KJ} is parallel to \overline{MN} .
 \overline{JN} is parallel to \overline{KM} .
7. Area = ℓw
 $= 13 \times 9$
 $= 117 \text{ in.}^2$
 The area of the rectangle is 117 square inches.
8. Area = ℓw
 $= 20 \times 14$
 $= 280 \text{ m}^2$
 The area of the rectangle is 280 square meters.
9. Area = ℓ^2
 $= 5 \times 5$
 $= 25 \text{ cm}^2$
 The area of the square is 25 square centimeters.
10. Area = ℓ^2
 $= 11 \times 11$
 $= 121 \text{ ft}^2$
 The area of the square is 121 square feet.
11. Base = $\overline{YZ} = 20 \text{ cm}$
 Height = $\overline{XW} = 15 \text{ cm}$
 Area of triangle = $\frac{1}{2}bh$
 $= \frac{1}{2} \cdot 20 \cdot 15$
 $= 150 \text{ cm}^2$
 The area of triangle XYZ is 150 square centimeters.
12. 84 square feet
13. 130 square meters
14. Base = $\overline{ST} = 8 \text{ in.}$
 Height = $\overline{RU} = 3.6 \text{ in.}$
 Area of triangle = $\frac{1}{2}bh$
 $= \frac{1}{2} \cdot 8 \cdot 3.6$
 $= 14.4 \text{ in.}^2$
 The area of triangle RST is 14.4 square inches.
15. 24 square feet
16. 37.8 square meters
17. Area of triangle $STU = \frac{1}{2}bh$
 $108 = \frac{1}{2} \cdot 24 \cdot h$
 $108 = 12 \cdot h$
 $108 \div 12 = 12 \cdot h \div 12$
 $9 = h$
 The height of triangle STU is 9 inches.

18. 20 centimeters
19. 24 feet
20. Area of triangle $GHJ = \frac{1}{2}bh$
 $286 = \frac{1}{2} \cdot b \cdot 26$
 $286 = \frac{1}{2} \cdot 26 \cdot b$
 $286 = 13 \cdot b$
 $286 \div 13 = 13 \cdot b \div 13$
 $22 = b$
 The base of triangle GHJ is 22 inches.
21. 16 centimeters
22. 14 meters

Lesson 10.2

1. Base = $\overline{GH} = 20 \text{ in.}$
 Height = $\overline{JK} = 12 \text{ in.}$
 Area of parallelogram $FGHJ = bh$
 $= 20 \cdot 12$
 $= 240 \text{ in.}^2$

The area of parallelogram $FGHJ$ is 240 square inches.

2. 48 square meters
3. 28.5 square centimeters
4. Height = $\overline{LM} = 20 \text{ in.}$
 Sum of bases = $\overline{HL} + \overline{JK}$
 $= 15 + 30$
 $= 45 \text{ in.}$

Area of trapezoid $HJKL$

$$= \frac{1}{2}h(b_1 + b_2)$$

$$= \frac{1}{2} \cdot 20 \cdot 45$$

$$= 450 \text{ in.}^2$$

The area of trapezoid $HJKL$ is 450 square inches.

5. 78 square centimeters
6. 162 square feet
7. Height = $\overline{GH} = 5 \text{ in.}$
 Sum of bases = $\overline{DG} + \overline{EF}$
 $= 5 + 9$
 $= 14 \text{ in.}$

Area of trapezoid $DEFG$

$$= \frac{1}{2}h(b_1 + b_2)$$

$$= \frac{1}{2} \cdot 5 \cdot 14$$

$$= 35 \text{ in.}^2$$

The area of trapezoid $DEFG$ is 35 square inches.

$$\begin{aligned}
 8. \text{ Area of trapezoid } WXYZ &= \frac{1}{2}h(b_1 + b_2) \\
 540 &= \frac{1}{2} \cdot h \cdot (22 + 38) \\
 540 &= \frac{1}{2} \cdot h \cdot 60 \\
 540 &= \frac{1}{2} \cdot 60 \cdot h \\
 540 &= 30 \cdot h \\
 540 \div 30 &= 30 \cdot h \div 30 \\
 18 &= h
 \end{aligned}$$

The height of trapezoid $WXYZ$ is 18 inches.

9. 34 meters

10. 23 feet

$$\begin{aligned}
 11. \text{ a) Area of trapezoid } CDEF &= \frac{1}{2}h(b_1 + b_2) \\
 832 &= \frac{1}{2} \cdot h \cdot (28.6 + 13) \\
 832 &= \frac{1}{2} \cdot h \cdot 41.6 \\
 832 &= \frac{1}{2} \cdot 41.6 \cdot h \\
 832 &= 20.8 \cdot h \\
 832 \div 20.8 &= 20.8 \cdot h \div 20.8 \\
 40 &= h
 \end{aligned}$$

The height of trapezoid $CDEF$ is 40 feet.

$$\begin{aligned}
 \text{b) Area of triangle } FDE &= \frac{1}{2}bh \\
 &= \frac{1}{2} \cdot 13 \cdot 40 \\
 &= 260 \text{ ft}^2
 \end{aligned}$$

The area of triangle FDE is 260 square feet.

Lesson 10.3

$$\begin{aligned}
 1. \text{ Area of triangle} &= \frac{1}{2}bh \\
 &= \frac{1}{2} \cdot 14 \cdot 9.6 \\
 &= 67.2 \text{ cm}^2
 \end{aligned}$$

Area of pentagon

$$\begin{aligned}
 &= 5 \cdot \text{area of triangle} \\
 &= 5 \times 67.2 \\
 &= 336 \text{ cm}^2
 \end{aligned}$$

The area of the pentagon is 336 square centimeters.

2. 97.5 square inches

$$\begin{aligned}
 3. \text{ Area of triangle} &= \frac{1}{2}bh \\
 &= \frac{1}{2} \cdot 20 \cdot 17.3 \\
 &= 173 \text{ cm}^2
 \end{aligned}$$

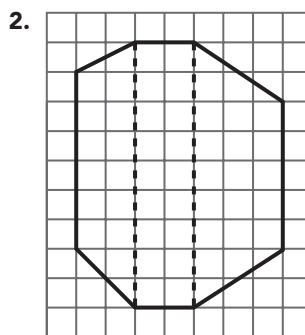
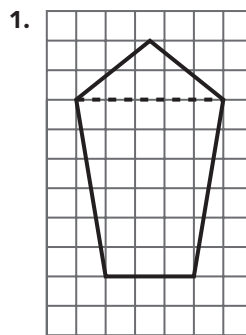
Area of hexagon

$$\begin{aligned}
 &= 6 \cdot \text{area of triangle} \\
 &= 6 \times 173 \\
 &= 1,038 \text{ cm}^2
 \end{aligned}$$

The area of the tablemat is 1,038 square centimeters.

4. 940.5 square inches

Lesson 10.4



$$\begin{aligned}
 3. \text{ a) Area of square} &= \ell^2 \\
 81 &= \ell^2 \\
 \sqrt{81} &= \ell \\
 9 &= \ell \\
 \text{Area of triangle} &= \frac{1}{2}bh \\
 &= \frac{1}{2} \cdot 15 \cdot 9 \\
 &= 67.5 \text{ ft}^2
 \end{aligned}$$

The area of the triangle NPQ is 67.5 square feet.

$$\begin{aligned}
 \text{b) Area of trapezoid } MPQR &= \text{area of square } MNQR \\
 &\quad + \text{area of triangle } NPQ \\
 &= 81 + 67.5 \\
 &= 148.5 \text{ ft}^2
 \end{aligned}$$

The area of trapezoid $MPQR$ is 148.5 square feet.

4. a) 7 inches

b) 49 square inches

c) 105 square inches

$$\begin{aligned}
 5. \text{ Area of trapezoid } STVY &= \frac{1}{2}h(b_1 + b_2) \\
 242 &= \frac{1}{2} \cdot h \cdot (18 + 18 + 8) \\
 242 &= \frac{1}{2} \cdot h \cdot 44 \\
 242 &= \frac{1}{2} \cdot 44 \cdot h \\
 242 &= 22 \cdot h \\
 242 \div 22 &= 22 \cdot h \div 22 \\
 11 &= h
 \end{aligned}$$